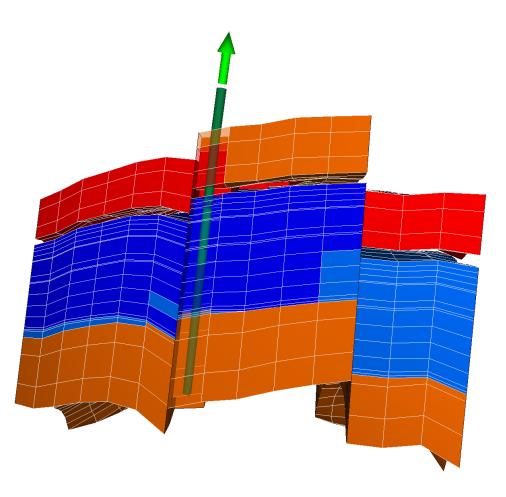
## Impact of mesh partitioning on parallel OPM Flow performance

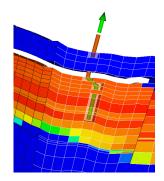
**Andreas Thune** 

August 2022

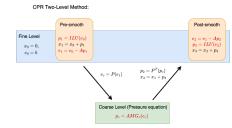


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This presentation focuses on distributed wells and improvements in OPM Flows parallel performance.



New edge-weighting scheme utilizing distributed well implementation.



Avoiding non-contributing computations in the CPR preconditioner.

Reservoir mesh is partitioned by first translating it to an edge-weighted graph.

$$\Omega \to G = (V, E, \omega: E \to \mathbb{R})$$

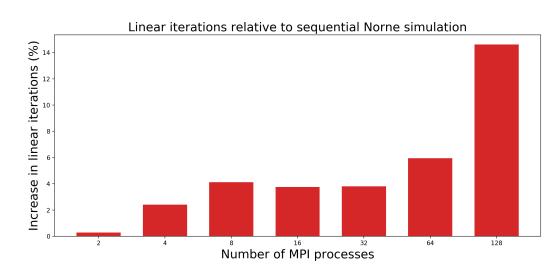
$$P\text{-way graph partitioning problem}$$

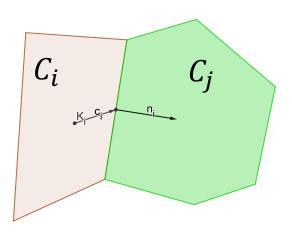
$$\min_{c} \left( J(\mathcal{C}) = \sum_{e \in \mathcal{C}} \omega(e) \right),$$
Subject to: 
$$\frac{P \cdot \max_{i}(|V_{i}|)}{\sum_{i}|V_{i}|} < \epsilon.$$

## Transmissibility edge-weights are used to yield good linear solver convergence.

### Transmissibility and well edge weights:

$$\omega(e) = \begin{cases} T_e, & e \text{ is face edge,} \\ \infty, & e \text{ is well edge.} \end{cases}$$





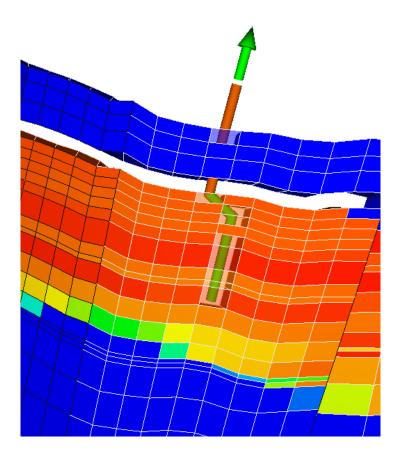
Transmissibility:  

$$T_{ij} = \left(\frac{1}{t_i} + \frac{1}{t_j}\right)^{-1} t_i = \frac{\vec{c}_i K_i \vec{n}_i}{||\vec{c}_i||^2}$$

### Well edge-weights ensure that wells remain on single subdomain.

### Transmissibility and well edge weights:

$$\omega(e) = \begin{cases} T_e, & e \text{ is face edge,} \\ \infty, & e \text{ is well edge.} \end{cases}$$



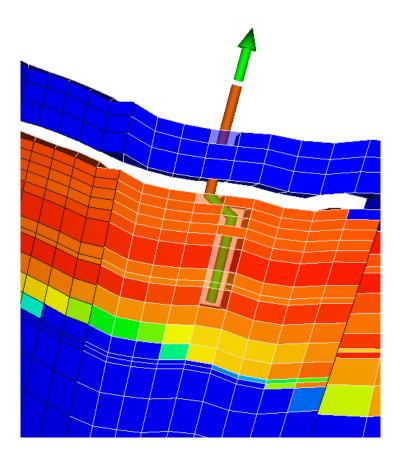
## Well edge-weights ensure that wells remain on single subdomain.

### Transmissibility and well edge weights:

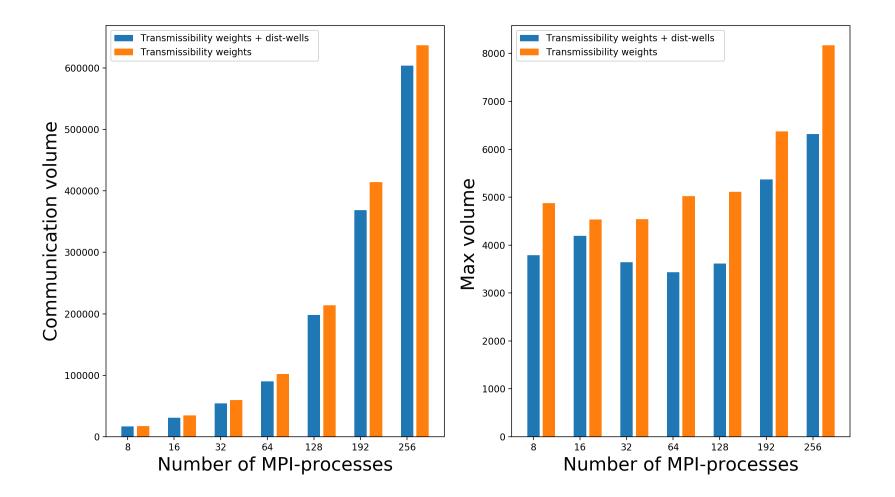
$$\omega(e) = \begin{cases} T_e, & e \text{ is face edge,} \\ \mathbf{0}, & e \text{ is well edge.} \end{cases}$$

#### Why 0-weighted well edges:

- Infinity well edge-weights creates poor quality partitions.
- Well contributions are not<sup>\*</sup> added to preconditioner matrix.

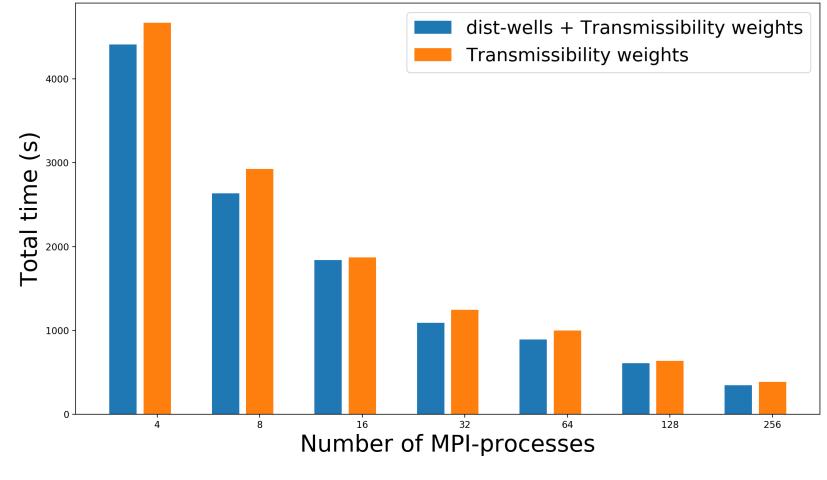


## Partitioning without well edge-weights reduces total communication volume.



Case: 1-millon cell black-oil case.

Distributed wells partitioning results in reduced Flow simulation execution time on 1-million cell black-oil case.



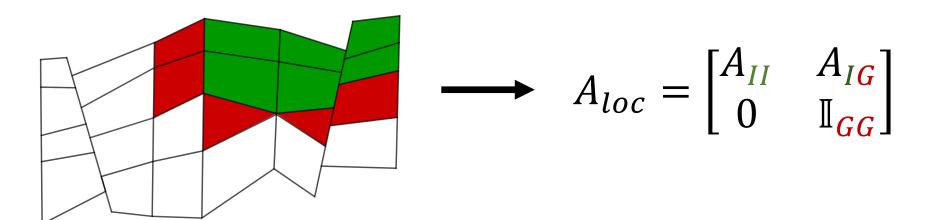
- Case: 1-millon cell black-oil case.
- ILUO and default settings.
- CPU: Dual-32 core AMD EPYC Naples.

# Ghost cells allows for communication free system assembly.

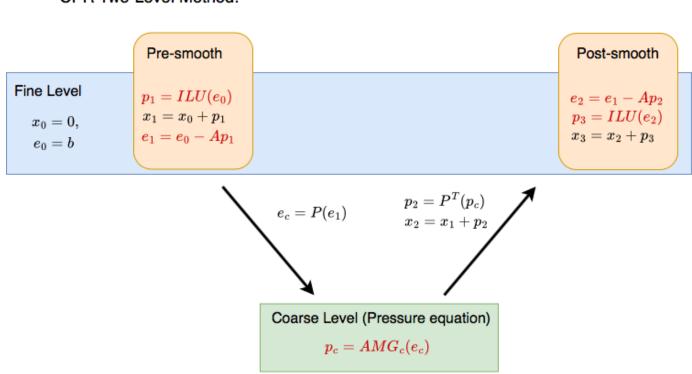
Local grid:

- Green interior cells.
- Red ghost cells.

Assembled local system:

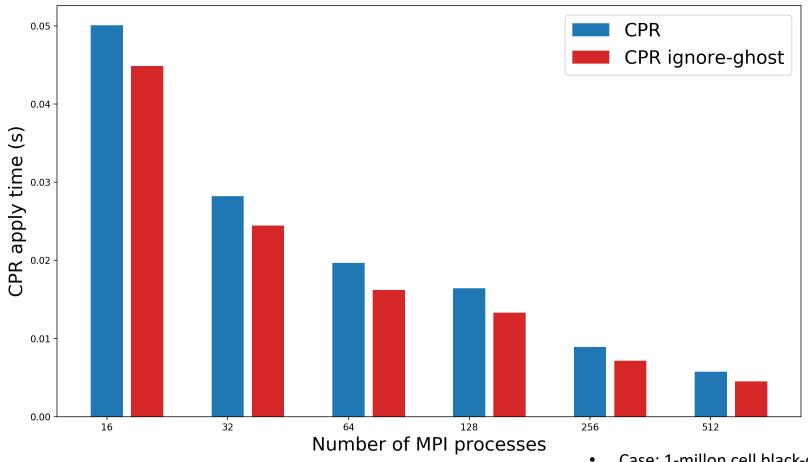


### Matrix-vector multiplication and smoother operations in CPR and AMG benefit from removing ghost-DoF computations.



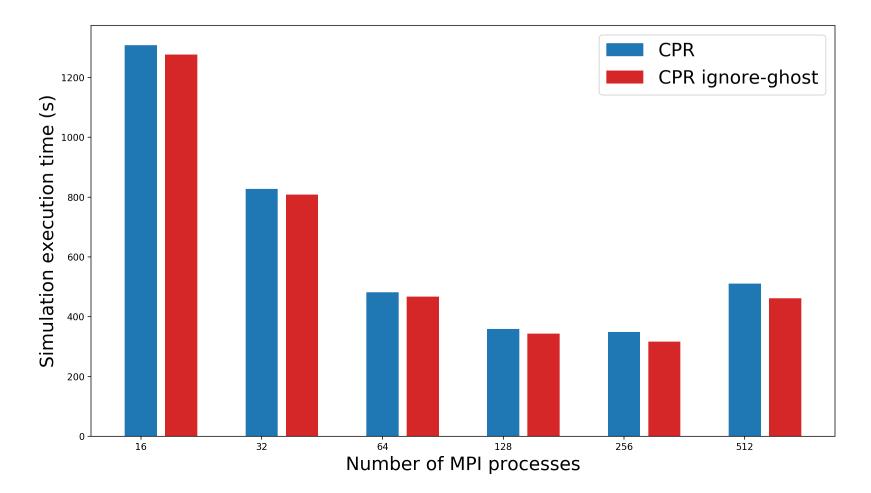
CPR Two-Level Method:

# CPR apply time is reduced by 10-20% when ignoring ghost DoFs.



- Case: 1-millon cell black-oil case.
- CPU: Dual-64 core AMD EPYC Milan.

# Flow execution time on 1-millon black-oil case is reduced by 5-10% when ignoring ghost DoFs in CPR.



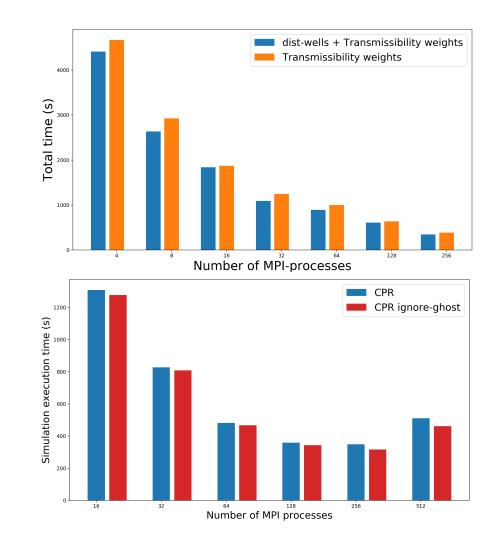
- Case: 1-millon cell black-oil case.
- CPU: Dual-64 core AMD EPYC Milan.

# In summary, partitioning edge-weighting strategy impacts OPM Flow performance.

**Questions?** 

Distributed well implementation can improve partitioning quality and overall performance.

Avoiding non-contributing ghost computations reduce CPR execution time.



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